

## Notes – Properties of Logarithms

**\*Note that for all of these properties, the logarithms must have the same base!**

**Product Property:** The logarithm of a product is the sum of the logarithms of its factors. (Add)

Examples:  $\log_2 3 \cdot 4 = \log_2 3 + \log_2 4$  OR  $\log_5 6 + \log_5 x = \log_5 6x$

In a generalized symbolic form:  $\log_b mn = \log_b m + \log_b n$

**You try.** Rewrite the following:    1.  $\log_{12} 7 \cdot 3 =$                       2.  $\ln 5 + \ln y =$

\_\_\_\_\_

**Quotient Property:** The logarithm of a quotient is the difference of the logarithms of the numerator and the denominator. (Subtract)

Examples:  $\log_3 \frac{5}{7} = \log_3 5 - \log_3 7$  OR  $\log x - \log(2x - 3) = \log \frac{x}{2x - 3}$

In a generalized symbolic form:  $\log_b \frac{m}{n} = \log_b m - \log_b n$

**You try.** Rewrite the following:    1.  $\log_{12} \frac{7}{3} =$                       2.  $\log 5x - \log 13$

\_\_\_\_\_

**Power Property:** The logarithm of a power is the product of the logarithm and the exponent. (Bring the exponent out front).

Examples:  $\log_4 6^2 = 2\log_4 6$  OR  $4\ln x = \ln x^4$

In a generalized symbolic form:  $\log_b m^p = p \log_b m$

**You try.** Rewrite the following:    1.  $\log_{15} 5^3 =$                       2.  $8\log_3 2 =$

---